SOBUKHAZI HIGH SCHOOL

GENERAL CERTIFICATE OF EDUCATION ADVANCED LEVEL

STATISTICS 6046/2

JULY 2019 SESSION

Additional Materials

- Answer paper
- Graph paper
- List of formulae
- Scientific calculator

Time 3 hours

INSTRUCTION TO CANDIDATES

Write your name on all answer scripts.

Answer **all** questions in Section A and **any five** questions from Section B.

If a numerical answer cannot be given exactly, and the accuracy required is not specified in the question, then in the case of an angle it should be given correct to the nearest degree, and in other cases it should be given correct to 2 significant figures.

INFORMATION FOR CANDIDATES

The number of marks is given in brackets [ ] at the end of each question or part question.

The total number of marks for this paper is 120

Questions are printed in the order of their mark allocations.

The use of a scientific calculator is expected, where appropriate.

You are reminded of the need for clear presentation in your answers.

Section A [40 Marks]

Answer **all** questions in this section.

Question 1

a. Briefly explain what is meant by the following:

i. Discrete data

ii. Continuous data. [3]

b. A stem plot below gives ages for 20 people in a community.

Stem	Leaf
5	9
6	1 4 7 8 9
7	2 3 3 4 5 6 6 6 7 8
8	0 3 3 4 5

Key : 5|9 means 59

i. Calculate the age range of the distribution

ii. Illustrate the information on a box and whisker plot. [5]

Question 2

a) State the differences between a permutation and a combination. [2]

b) Two fuses are selected simultaneously and at random from a packet containing 5 good and 3 faulty fuses.

Find the number of ways of selecting

i. The 2 fuses from the packet

ii. One good and one faulty fuse from the packet.

iii. Hence or otherwise find the probability that exactly one faulty fuse is selected. [6]

Question 3

a) Explain what is meant by the following

i. Mutually exclusive events

ii. Independent events

[2]

b) A shop stocks tinned cat food of two makes, A and B, and two sizes, large and small.

Of the stock, 70% is of brand A, and 30% is of brand B. of the tins of brand A, 30% are small size whilst of the tins of brand B, 40% are small size.

Using a tree diagram, or otherwise, find the probability that

i. A tin chosen at random from the stock will be of small size.

ii. A small tin chosen at random from the stock will be of brand A. [6]

Question 4

The discrete random variable X has probability function

$$P(X=x) = \begin{cases} \dfrac{kx}{x^2+1}, & x = 2, 3 \\ \dfrac{2kx}{x^2-1}, & x = 4, 5 \\ 0, & \text{otherwise} \end{cases}$$

a. Show that the value of k is $\dfrac{20}{33}$ [2]

b. Find

i. The probability that X is less than 3 or greater than 4 [2]

ii. E(X) [2]

iii. Var(X) [2]

Question 5

A continuous variable X is distributed at random between the values x = 0 and x = 2, and has a probability density function $\boldsymbol{ax^2 + bx.}$ The mean is 1.25.

a. Show that $b = \frac{3}{4}$ and find the value of a. [3]

b. Find the variance of X. [3]

c. Verify that the median value of X is approximately 1.3 [2]

Section B [80 Marks]

Answer **any five** questions from this section.

Each question carries 16 marks.

Question 6

a. The probability that a fisherman has a successful day's fishing is 0.6. Given that he fishes for six days ever week, find the probability that in any week he has

i. Exactly four successful days. [2]

ii. At least two successful days [3]

The fisherman fishes for six days every week for many weeks. Estimate the mean and standard deviation of the number of successful days per week over the period. [3]

b. A shop sells a particular make of radio at a rate of four per week on average. The number sold in a week has a Poisson distribution.

i. Find the probability that the shop sells exactly three in a week. [2]

ii. Find the probability that the shop sells at least two in a week. [3]

iii. Find the smallest number that can be in stock at the beginning of the week in order to have at least a 99% chance of being able to meet all the demands during that week. [3]

Question 7

A car manufacturer is testing the braking distance for a new model of a car. The table shows the braking distance, *y metres*, for different speeds, *x km/h*, when the brakes were applied.

Speed of car (x km)	30	50	70	90	110	130
Braking distance (y metres)	25	50	85	155	235	350

Given that $\sum x = 480$, $\sum x^2 = 45\,400$, $\sum y = 900$, $\sum y^2 = 212\,100$ and $\sum xy = 94\,500$,

a. Plot a scatter diagram and comment on the relationship between the two sets of data. [4]

b. Calculate the product moment correlation coefficient and comment. [4]

c. Calculate the equation of the regression line ***y on x***. [4]

d. Use your equation to predict the value of

i. Y when x = 100

ii. Y when x = 150 [4]

Question 8

a. The time taken by the postman to deliver letters is normally distributed with a mean of 12 minutes and a standard deviation of 2 minutes. Estimate the number of days during the year when he takes

i. Longer than 17 minutes [2]

ii. Less than 10 minutes [2]

iii. Between 9 and 13 minutes. [2]

b. State conditions under which the binomial distribution can be approximated by a normal distribution. [2]

c. A particular hospital records show that each day on average, only 80% of people keep their appointment at the outpatients' clinic. Find the probability that on a day when 200 appointments have been booked,

i. More than 170 patients keep their appointments [4]

ii. At least 155 patients keep their appointments. [4]

Question 9

a. A random sample of 100 observations from a population with mean μ and standard deviation δ gave the following

$$\sum(x-50) = 123.5 \qquad \sum(x-50)^2 = 238.4$$

i. Calculate the unbiased estimates of the population mean μ and variance δ^2 [4]

ii. Find a 97% confidence interval for μ [4]

iii. Find $P(\dot{x} > 51)$ [2]

b. A company receives on average 6 orders per day. Find the probability that

i. No more than 2 orders will be received on a given day. [3]

ii. On a given half day, no orders will be received. [3]

Question 10

a. Distinguish between Type I and Type II errors as used in hypothesis testing. [2]

b. State the Central Limit Theorem. [2]

c. The management of a large hospital states that the mean age of its patients is 45 years. Records of a random sample of 100 patients give a mean age of 48.4 years. Using a population standard deviation of 18 years, test at the 5% significance level whether there is evidence that the management's statement is incorrect. State clearly your null and alternative hypotheses. [12]

Question 11

A random sample of 100 people was asked for their opinions about the amount of sport shown on TV. Each person had to say whether there was too much sport shown, about the right amount or not enough the numbers of men and women making each response are shown in the table.

	Men	Women
Too much sport	13	26
About right	22	22
Not enough sport	12	5

The null hypothesis is that a person's opinion about the amount of sport shown on TV is independent of the person's sex.

i. Construct a table showing the expected frequencies, assuming that the null hypothesis is true. [4]

ii. Use a chi squared test to test this null hypothesis, using a 5% significance level. Show full details of your method and state your conclusion clearly. [12]

Question 12

a. Define the terms
   i. Time series
   ii. Trend

b. The following are monthly sales ($) for a company for the months of January to October.

Month	Sales ($)
January	700
February	200
March	300
April	800
May	400
June	500
July	1000
August	500
September	600
October	1200

i. Plot the time series graph. [4]
ii. Describe the trend. [2]
iii. Calculate the 3 point moving average and plot it on the same graph. [6]
iv. Name any one method used to isolate the trend. [1]

ENDS